

## Corrigé type

### Exercice 1 (8 Points)

$$1 - \vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \rightarrow \begin{vmatrix} \hat{a}_x & \hat{a}_y & \hat{a}_z \\ \frac{\partial}{\partial x} & 0 & 0 \\ 0 & 0 & E_z \end{vmatrix} = -\frac{d}{dt} (B_x \hat{a}_x + B_y \hat{a}_y + B_z \hat{a}_z) \quad (1)$$

$$\begin{cases} 0 = -\frac{dB_x}{dt} \\ -\frac{\partial E_z}{\partial x} = -\frac{dB_y}{dt} \\ 0 = -\frac{dB_z}{dt} \end{cases} \rightarrow \begin{cases} B_x = 0 \\ B_y = \int \frac{\partial E_z}{\partial x} dt \\ B_z = 0 \end{cases} \rightarrow \begin{cases} B_x = 0 \quad (1) \\ B_y = -\frac{E_0}{C} \cos(\omega t - kx) \quad (1) \\ B_z = 0 \quad (1) \end{cases}$$

$$2 - \vec{R} = \vec{E} \times \vec{H} = \frac{\vec{E} \times \vec{B}}{\mu_0} = \frac{1}{\mu_0} \begin{vmatrix} \hat{a}_x & \hat{a}_y & \hat{a}_z \\ 0 & 0 & E_z \\ 0 & B_y & 0 \end{vmatrix} \rightarrow \vec{R} = \frac{E_0^2}{\mu_0 C} \cos^2(\omega t - kx) \hat{a}_x \quad (1)$$

$$3 - P = \iint_S \vec{R} \cdot d\vec{S} = \iint_S \|\vec{R}\| \cdot \hat{a}_x \cdot dS \hat{a}_x = \|\vec{R}\| \cdot S \quad (1) \quad \langle P \rangle = \frac{1}{T} \int_0^T P \cdot dt \rightarrow$$

$$\langle P \rangle = \frac{1}{T} \int_0^T \|\vec{R}\| \cdot S \cdot dt = \frac{E_0^2 \cdot S}{\mu_0 C} \cdot \frac{1}{T} \int_0^T \cos^2(\omega t - kx) \cdot dt \rightarrow \langle P \rangle = \frac{E_0^2 \cdot S}{2 \mu_0 C} \quad (1)$$

$\int_0^T \cos^2(\omega t - kx) \cdot dt = \frac{T}{2}$

### Exercice 2 (8 Points)

$$1 - \lambda = \frac{c}{f} = \frac{3 \cdot 10^8}{5,8 \cdot 10^9} \approx 0,052 \text{ m.} \quad (P_R)_{dB} = (P_R)_{dBm} - 30 = -85 - 30 = -115 \text{ dB}$$

$$P_R = P_T + G_T + G_R - L_S \rightarrow L_S = P_T + G_T + G_R - P_R = -10 + 16 + 16 + 115 = 137 \text{ dB} \quad (1)$$

$$(L_S)_{dB} = 20 \log\left(\frac{4\pi d}{\lambda}\right) \rightarrow d_{max} = \frac{\lambda}{4\pi} \cdot 10^{\frac{L_S}{20}} \quad (1) \quad \text{A.N} \rightarrow d_{max} = \frac{0,052}{4 \times 3,14} \cdot 10^{\frac{137}{20}} \rightarrow$$

$$d_{max} \approx 29 \text{ km.} \quad (1)$$

$$2 - r = \sqrt{\frac{\lambda d_1 d_2}{d_1 + d_2}} \text{ à mi-portée } d_1 = d_2 = \frac{d}{2} \rightarrow r = \frac{1}{2} \sqrt{\lambda d} \quad (0,5)$$

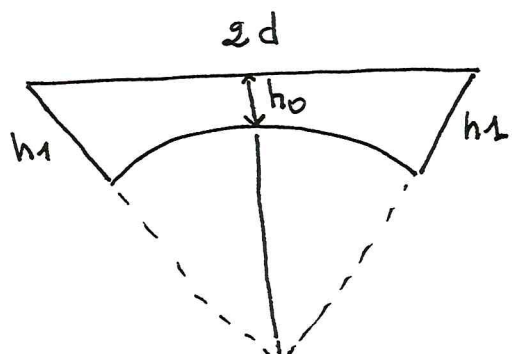
$$\text{A.N.} \rightarrow r = \frac{1}{2} \sqrt{0,05 \times 29 \times 10^3} \rightarrow r \approx 19 \text{ m.} \quad (0,5)$$

$$- \text{La hauteur des antennes } h = h_0 + r \text{ avec } h_0 = \frac{d^2}{8r} \text{ et } r = \frac{1}{2} \sqrt{\lambda d} = 19 \text{ m} \quad (0,5)$$

$$h_0 = \frac{29^2 \times 10^6}{8 \times 6,4 \times 10^6} \rightarrow h_0 = 16,4 \text{ m} \rightarrow h = h_0 + r \approx 16 + 19 = 35 \text{ m.} \quad (0,5)$$

### Exercice 3 (4 Points)

1 - Il faut que  $h_p \gg h_1 + r$   
 $h_1$ : hauteur des antennes quand l'axe radioélectrique est tangent à l'obstacle.



$r$ : rayon du 1<sup>er</sup> ellipsoïde de Fresnel dans le plan de l'obstacle.

$$(h_1 + R)^2 = (h_0 + R)^2 + d^2 \text{ où } R = \frac{4}{3} R_0 \text{ (atmosphère standard)}$$

$$2h_1 R \approx 2h_0 R + d^2 \rightarrow h_1 = h_0 + \frac{d^2}{2R} \quad (1)$$

$$r = \sqrt{\frac{\lambda d_1 d_2}{d_1 + d_2}}; \text{ ici } d_1 = d_2 = d \rightarrow r = \sqrt{\frac{\lambda d}{2}} \rightarrow \text{il faut que}$$

$$h_p \gg h_1 + \sqrt{\frac{\lambda d}{2}} \quad (1)$$

$$\text{2 - } d = 15 \times 10^3 \text{ m. } R = \frac{4}{3} \times 6400 \times 10^3 \text{ m; } h_0 = 40 \text{ m;}$$

$$\frac{d^2}{2R} = 13,2 \text{ m. } h_p = 90 \text{ m.}$$

$$h_p > h_1 + \sqrt{\frac{\lambda d}{2}} \rightarrow \sqrt{\frac{\lambda d}{2}} \leq h_p - h_1 \rightarrow \frac{\lambda d}{2} \leq (h_p - h_1)^2 \rightarrow$$

$$\lambda = \frac{c}{f} \leq (h_p - h_1)^2 \times \frac{2}{d} \rightarrow f \geq \frac{c \cdot d}{2(h_p - h_1)^2} \quad (1)$$

$$\text{Soit: } f_{\min} = \frac{c \cdot d}{2(h_p - h_1)^2}. \text{ A.N.} \rightarrow f_{\min} = \frac{3 \cdot 10^8 \times 15 \times 10^3}{2 \cdot (90 - 40 - 13,2)^2} \rightarrow$$

$$f_{\min} \approx 1,66 \text{ GHz. } (1)$$